

If you're reading this, please contribute!

REMINDER! This is a template! The cheat sheet maintainer (.json) intentionally leaves extra space for you to add your own notes! If something's missing, add it yourself! (and if it's important enough please contribute!)

FSP

Syntax

```
// instance prefixing - a:P
SWITCH = (on -> off -> SWITCH).
||TWO_SWITCH = (a:SWITCH || b:SWITCH).

// relabeling - /new1/old1, new2/old2, ...
CLIENT = (call -> wait -> continue -> CLIENT).
SERVER = (request -> service -> reply -> SERVER).
||CLIENT_SERVER = (CLIENT||SERVER)/(call/request,
    -> reply/wait).

// process prefixing (mutex) - {a1,..., ax} :: P
RESOURCE = (acquire -> release RESOURCE).
USER = (acquire -> user -> released -> USER).
||RESOURCE_SHARE = (a:USER || b:USER || {a, b}:
    -> RESOURCE).

// RESOURCE is a single shared instance between
// the two USERS

// for loop syntax
|| SWITCHES (N = 3) = (forall {i:1..N} s[i]:SWITCH
    -> )

// or alternatively
range Seats = 1..3
|| SEATS=(seat[i:1..3]:SEAT).

// hiding operator - \{a1, ..., ax\}
// interface operator - @\{a1, ..., ax\}
// these two do the same thing
USER = (acquire -> use -> release -> USER)\{use}.
USER = (acquire -> use -> release -> USER)@\{use
    -> acquire, release\}.

// syntax for progress
progress P = {a1, ..., an}
// syntax for high priority
||C = (P||Q)<{a1, ..., an}.
// syntax for low priority
||C = (P||Q)>{a1, ..., an}.
// simulating a boolean
const False = 0
const True = 1
range Bool = 0..1
```

Marker-user example

```
MAKER = (make -> ready -> MAKER).
USER = (ready -> user -> USER).
||MAKER_USER = (MAKER || USER).
```

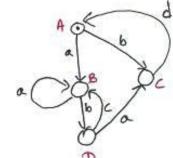
Garden example (maybe move this to a diff section later)

```
const N = 4
range T = 0..N
set VarAlpha = {value.(read[T], write[T])}
VAR = VAR[0],
VAR[u:T] = (read[u] -> VAR[u]
    | write[v:T] -> VAR[v]).
TURNSTILE = (go -> RUN,
RUN = (arrive -> INCREMENT
    | end -> TURNSTILE),
INCREMENT = (value.read[x:T]
    -> value.write[x+1]->RUN
    |+VarAlpha).

DISPLAY = (value.read[T]->DISPLAY)+(value.write[T
    -> ]).

||GARDEN = (east:TURNSTILE || west:TURNSTILE ||
    -> display:DISPLAY
    || {east,west,display}::value:VAR
    /{go /{east,west}.go,
    end/{east,west}.end}.
```

LTS



$A = (a \rightarrow B \mid b \rightarrow C)$
 $B = (a \rightarrow B \mid b \rightarrow D)$
 $C = (d \rightarrow A)$
 $D = (a \rightarrow C \mid c \rightarrow B)$

Bounded Buffer

A buffer with a fixed number of slots

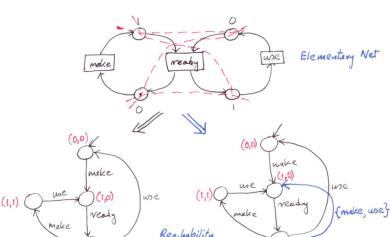
```
BUFFER(N=5) = COUNT[0],
COUNT[i:0..N] = (when (i<N) put->COUNT[i+1]
    | when (i>0) get->COUNT[i-1]
    | ).

PRODUCER = (put->PRODUCER).
CONSUMER = (get->CONSUMER).

||BOUNDEDBUFFER = (PRODUCER || BUFFER(5) || CONSUMER).
```

Petri Nets

Reachability Graphs



Hiding/Labeling

relabeling: (PROCESS) \{newlabel/oldlabel, ..., newlabeln/oldlabeln\} hides all actions except a1 ... ax

hiding: (PROCESS) \{a1...an\} hides actions a1...an

$\{a1, \dots, ax\} :: P$ replaces every action label n in the alphabet of P with the labels a1..n, ..., ax..n. Thus, every transition (n -> X) in the definition of P is replaced with the transitions $\{a1..n, \dots, ax..n\} \rightarrow X$

Bisimulation

State Bisimilarity – $p \approx q$ iff whatever action executed at p can also be executed at q, and vice versa.

LTS Bisimilarity – $P \approx Q$ iff each state p_t is bisimilar to an appropriate state q_t that is reachable from the initial state by the same trace t in Q .

Mutual Exclusion

Arbitrary interleaving of read and write actions leads to **interference**. Interference bugs are difficult to locate. We use **mutual exclusion** to only give one process access to the shared resource at a time.

LOCK = (acquire -> release -> LOCK).

U1 = (acquire -> use -> release -> U1).
U2 = (acquire -> use -> release -> U2).
||SYSTEM = (u1:U1||u2:U2||{u1,u2}:LOCK).

Above allows for lock-use-release for either user but only one of them at a time.

Monitors and Semaphores

Monitor – A threadsafe class where each function is wrapped by a mutex. Essentially, only one process may access the class at a time. Entirely syntactic sugar. **Semaphore** – Essentially a mutex with a queue of processes

```
down(s): if s > 0 then
    decrement s
else
    block execution of calling process
up(s): if processes blocked on s then
    awaken one of them
else
    increment s
```

```
const Max = 0
range Int = 0..Max
SEMAPHORE(N=0) = SEMA[N],
SEMA[v:Int] = (up->SEMA[v+1]
    | when(v>0) down->SEMA[v-1]
    | ).

LOOP = (mutex.down -> critical -> mutex.up -> LOOP
    -> ).

||SEMADEMO = (p1..3):LOOP || (p1..3)::mutex:
    -> SEMA(1)).
```

Bounded Buffer

A buffer with a fixed number of slots

```
BUFFER(N=5) = COUNT[0],
COUNT[i:0..N] = (when (i<N) put->COUNT[i+1]
    | when (i>0) get->COUNT[i-1]
    | ).

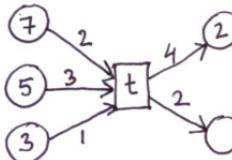
PRODUCER = (put->PRODUCER).
CONSUMER = (get->CONSUMER).

||BOUNDEDBUFFER = (PRODUCER || BUFFER(5) || CONSUMER).
```

Nested Monitor Problem

P/T nets

Each place in a P/T net can hold multiple tokens. Each transition has a weight, w, associated with it. If it is an input transition, firing takes w tokens from the input place. If its an output transition, firing adds w tokens to the output place. An action can only be fired if enough input tokens are present in all input



places.

Deadlocks

Dining Philosophers Problem

Simple minded construction:

```
FORK = (get -> put -> FORK).
PHIL = (think -> right.get -> left.get -> eat ->
    right.put -> left.put -> PHIL).
||DINERS(N = 5) = forall{i:1..N} (phil[i] : PHIL
    -> || (phil[i].right, phil[(i % 5) + 1].
    -> left) :: FORK
```

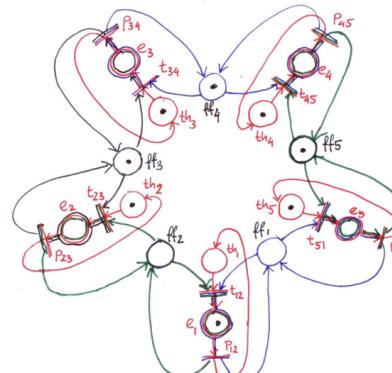
Solution 1 – Add asymmetry into the composition, where 1, 3, 5 always perform left.get -> right.get, while 2, 4 always perform right.get -> left.get.

```
PHIL = (when(i=1|i=3|i=5) think -> left.get ->
    right.get -> eat -> left.put -> right.
    -> put -> PHIL).
||when(i=2|i=4) think -> right.get -> left.
    -> get -> eat -> right.put -> left.
    -> put -> PHIL).
```

Solution 2 – Use a butler to prevent more than 4 philosophers from sitting at the table.

```
PHIL = (think -> sitdown -> right.get -> left.get
    -> eat -> right.put -> left.put ->
    get -> PHIL).
BUTLER(K=4) = COUNT[0],
COUNT[i|i<4] = (when(i<K) sitdown -> COUNT[i+1]
    -> getup -> COUNT[i-1]).
||DINERS(N=5) ... ||(phil[i:1..N]):BUTLER(K=4).
```

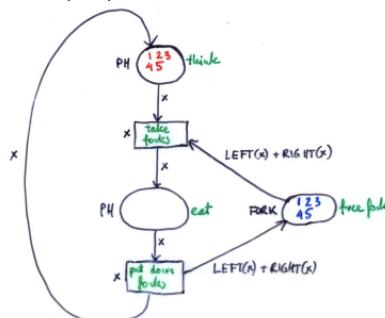
Solution 3 – Use Simultaneity



Only fire a transition if both forks are available

Coloured Petri Nets

“Colours” are simply types of tokens that are passed around the petri net. Paths to transitions are either labeled with variables or functions that transform one of the input variables into the object to remove from a state.



```
||RESOURCES = ({s_m,s_p}):TOBACCO || {s_t,s_m}::PAPER || {s_t,s_p}::MATCH:
||AGENT_RULE = ({s_m,s_p,s_t}):RULE || ({s_m,s_p}):AGENT_P || ({s_t,s_p}):AGENT_M.
||CIG_SMOKERS = (SMOKERS || RESOURCES || AGENT_RULE) / ({s_t}.get_paper/{s_t}.picked,
{s_m}.get_paper/{s_m}.picked,
{s_p}.get_paper/{s_p}.picked,
{s_t}.deliver_paper/{s_t}.delivered,
{s_m}.deliver_paper/{s_m}.delivered,
{s_p}.deliver_paper/{s_p}.delivered,
{s_t}.smoking_completed/{s_t}.smoke_cigarette,
{s_m}.smoking_completed/{s_m}.smoke_cigarette,
{s_p}.smoking_completed/{s_p}.smoke_cigarette).
```

Property (safety)

```
property CORRECT_PICKUP = ({s_t}.get_paper->{s_t}.get_match->CORRECT_PICKUP
    || {s_p}.get_tobacco->{s_p}.get_match->CORRECT_PICKUP
    || {s_m}.get_tobacco->{s_m}.get_paper->CORRECT_PICKUP).
```

Ask first, do later

```
SMOKER_T=( no_tobacco -> get_paper -> get_match->
    roll_cigarette -> smoke_cigarette -> SMOKER_T)
SMOKER_P=( no_paper -> get_tobacco -> get_match->
    roll_cigarette -> smoke_cigarette -> SMOKER_P)
SMOKER_M=( no_match -> get_tobacco -> get_paper->
    roll_cigarette -> smoke_cigarette -> SMOKER_M)
TOBACCO = ( delivered -> picked -> TOBACCO )
PAPER = ( delivered -> picked -> PAPER )
MATCH = ( delivered -> picked -> MATCH )
AGENT_T = ( can_deliver -> no_tobacco -> deliver_paper->deliver_match->AGENT_T)
AGENT_P = ( can_deliver -> no_paper -> deliver_match->deliver_tobacco->AGENT_P)
AGENT_M = ( can_deliver -> no_match -> deliver_tobacco->deliver_paper->AGENT_M
    -> )
RULE = ( can_deliver -> smoking_completed -> RULE )
SMOKERS = {s_t}:SMOKER_T || {s_p}:SMOKER_P || {s_m}:
    -> SMOKER_M
RESOURCES = ({s_m,s_p}):TOBACCO || {s_t,s_m}:PAPER
|| {s_t,s_p}:MATCH
AGENT_RULE = ({s_m,s_p,s_t}):RULE || ({s_m,s_p}):AGENT_P || ({s_t,s_p}):AGENT_M
CIG_SMOKERS = (SMOKERS || RESOURCES || AGENT_RULE)
    -> / ({s_t}.get_paper/{s_t}.picked,
{s_m}.get_paper/{s_m}.picked,
{s_p}.get_paper/{s_p}.picked,
{s_t}.deliver_paper/{s_t}.delivered,
{s_m}.deliver_paper/{s_m}.delivered,
{s_p}.deliver_paper/{s_p}.delivered,
{s_t}.smoking_completed/{s_t}.smoke_cigarette,
{s_m}.smoking_completed/{s_m}.smoke_cigarette,
{s_p}.smoking_completed/{s_p}.smoke_cigarette).
```

Multidimensional Semaphores of Agarwala

edown

up

npdown

ndown

C

nup

up(s)

down(s)

edown(s)

up(s)

npdown(s)

ndown(s)

C

nup

up(s)

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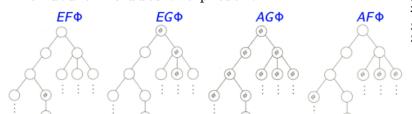
C

nup

CTL and LTL

CTL

A: along all paths
E: exists a path
X: next state
F: some future state
G: all future states
U: until ("killer" event must happen)
W: weak until ("killer" event may never happen).
 In CTL, must start with path operator (A/E). W in CTL: $A[p \wedge W q] \equiv A[p \vee u q] \vee AG p$ (same with E).
Common Patterns $AX\phi$ - in every next state.
 $EX\phi$ - in some next state.
 $AG\phi$ - All computation paths beginning with s the property ϕ holds Globally.
 $EG\phi$ - There Exists a path beginning in s such that ϕ holds Globally along the path.
 $AF\phi$ - For All computation paths beginning with s there will be some Future state where ϕ holds.
 $EF\phi$ - There Exists a computation path beginning in s such that ϕ holds in some Future states.
 $A[\phi_1 \wedge \phi_2]$ - All computation paths beginning in s satisfy that ϕ_1 Until ϕ_2 holds.
 $E[\phi_1 \wedge \phi_2]$ - There Exists a computation path beginning in s such that ϕ_1 Until ϕ_2 holds on it. The future includes the present.



Equivalences $\neg AF\phi \equiv EG\neg\phi$

$\neg EF\phi \equiv AG\neg\phi$

$\neg AX\phi \equiv EX\neg\phi$

$AF\phi \equiv A[TU\phi]$

$EF\phi \equiv E[TI\phi]$

Elevator Example 1

"An upwards travelling elevator at the second floor does not change direction when it has passengers wishing to go to the fifth floor"

CTL: $AG(floor = 2 \wedge direction = up \wedge \text{ButtonPressed}5 \Rightarrow A[direction = up \wedge floor = 5])$.

Elevator Example 2

"The elevator can remain idle on the third floor with its doors closed"

CTL: $AG((floor = 3 \wedge idle \wedge door = closed) \Rightarrow EG(floor = 3 \wedge idle \wedge door = closed))$

LTL

\perp - false, T - true Other symbols mean the same as above. A set of paths satisfies ϕ if every path in the set satisfies ϕ

Equivalences $\neg G\phi \equiv F\neg\phi$

$\neg F\phi \equiv G\neg\phi$

$\neg X\phi \equiv X\neg\phi$

$F(\phi \vee \psi) \equiv F\phi \vee F\psi$

$G(\phi \wedge \psi) \equiv G\phi \wedge G\psi$

$F\phi \equiv TU\phi$

$G\phi \equiv \perp R\phi$

$\phi U \psi \equiv \phi W \psi \wedge F\psi$

$\phi W \psi \equiv \phi U \psi \vee G\phi$

$\phi W \psi \equiv \phi R(\phi \vee \psi)$

$\phi R \psi \equiv \psi W(\phi \wedge \psi)$

Dynamic Systems

Golf Club Program

Players at a golf club borrow and then return golf balls. Different players need different numbers of balls. How do we model the infinite stream of players? We can only model infinite behaviours.

Adverse Scheduling

Intentionally schedule priorities to try to break things

For golf club scheduling:

progress NOVICE = {NOVICES.get[R]}
progress EXPERT = {EXPERTS.get[R]}

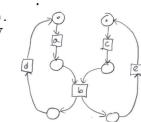
||ProgressCheck = GOLFCLUB >> {Players.put[R]}.

Q7 - A1

$P = (a \rightarrow b \rightarrow d \rightarrow P)$.
 $Q = (c \rightarrow b \rightarrow e \rightarrow Q)$.
 $||S1 = (P \parallel Q)$.

$S2 = (a \rightarrow S2A \mid c \rightarrow S2B)$,
 $S2A = (c \rightarrow b \rightarrow d \rightarrow S2C \mid c \rightarrow b \rightarrow e \rightarrow S2D)$,
 $S2B = (a \rightarrow b \rightarrow d \rightarrow S2C \mid a \rightarrow b \rightarrow e \rightarrow S2D)$,
 $S2C = (e \rightarrow S2 \mid a \rightarrow e \rightarrow S2A)$,
 $S2D = (d \rightarrow S2 \mid c \rightarrow d \rightarrow S2B)$.

For the above FSPs, they both share the same LTS diagram (LTS version of the right petri net), however, since $||S1$ has simultaneous actions, its petri net will be show simultaneity whereas $S2$ will not.



Q5 - Midterm

A central computer is connected to remote terminals, with seats for concert hall. Clients choose a free seat and clerk enters the seat into the system and gives a ticket. We need to prevent double booking while letting clients choose any available seat.

```
const False = 0
range True = 1
range Bool = False..True
SEAT = SEAT[False],
SEAT[reserved:Bool] = ( reserve > SEAT[True]
  | query[reserved] -> SEAT[reserved]
  | when (reserved) reserve -> ERROR // error
    | when (reserved) replace_toner-> PRINTER[j]
  )..
range Seats = 0..1
||SEATS = (seat[Seats]:SEAT).
LOCK = (acquire -> release -> LOCK).
TERMINAL = (choose[seats]:SEAT -> acquire
  -> seat[s].query[reserved:Bool]
  -> when (reserved) seat[s].reserve ->
    | when (reserved) release -> TERMINAL
  )..
set Terminals = {a, b}
||CONCERT = (Terminals:TERMINAL || Terminals::LOCK).
```

Q7 - Midterm

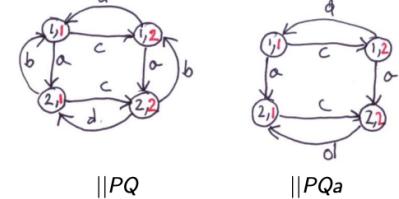
```
P1 = (a -> b -> c -> P1 | a -> c -> b -> P1).
P2 = (a -> (b -> c -> P2 | c -> b -> P2)).
Q = (b -> c -> Q).
||P1Q = (P1 || Q).
||P2Q = (P2 || Q).
```

For P1 there are two possible paths which have an a transition. For P2, it starts with one a transition, so both the starting states are equivalent in this case. In both branches of P1, you either do $b \rightarrow c \rightarrow P1$ or $c \rightarrow b \rightarrow P1$. For P2, it splits into two possible paths, $b \rightarrow c \rightarrow P2$ or $c \rightarrow b \rightarrow P2$, which is the same as the traces for P1. Therefore P1 and P2 are equivalent. For $||P1Q$ and $||P2Q$, both P1 and Q, and P2 and Q, share $b \rightarrow c$. In P1 and Q, this becomes a shared action and both P1 and Q will want to use the same transitions at the same time (deadlock). For $||P2Q$, the FSP can choose to go in the alternate direction instead of waiting for Q to finish, so this one would not have a deadlock whereas $||P1Q$ will have one.

Alphabet Extension Processes

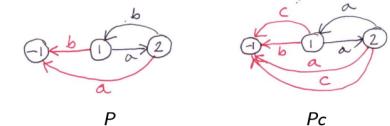
```
P = (a -> b -> d -> P).
Q = (c -> d -> Q).
Q = (c -> d -> Q) + (b).
```

When taking the composition of $||PQ$ and $||PQa$, we take the union of both processes and remove duplicate transitions. In the case of PQ, there are no similar transitions, however PQa shares the b transition, so that is removed from the LTS.



Properties

With properties, whenever you add more transitions through alphabet extension, you need to apply this transition to every state and use it as a transition to an error state.



Tut 6 Mutex Example

Workers in an office share a printer. The printer is able to print any number of jobs before it runs out of toner. This is replaced by a technician when necessary.

```
const J=3
range Jobs = 0..J
// j Represents toner
PRINTER = PRINTER [3] = (when j==0 replace_toner-> PRINTER[j])
|when j>0 print_job-> PRINTER[j-1].
USER = (print_job->USER).
const M = 2
range Users = 0..M
||USERS = (forall[i]:Users user [i]:USER).
TECHNICIAN=(replace_toner->TECHNICIAN).
||OFFICE=(USERS||PRINTER||TECHNICIAN)
/(user[Users].print_job/print_job)
range Seats = 0..1
||SEATS = (seat[Seats]:SEAT).
LOCK = (acquire -> release -> LOCK).
TERMINAL = (choose[seats]:SEAT -> acquire
  -> seat[s].query[reserved:Bool]
  -> when (reserved) seat[s].reserve ->
    | when (reserved) release -> TERMINAL
  )..
set Terminals = {a, b}
||CONCERT = (Terminals:TERMINAL || Terminals::LOCK).
```

Binary Semaphore Question

In an operating system, a binary semaphore is used to control access to the console. The console is used by user and system processes. Write down a model with FSP for this system. Discuss when user processes may be denied access to the console.

```
BSEMA = (up -> down -> BSEMA).
PROCESS = (console.up -> console.down -> PROCESS).
set Processes = {user[1..2],system[1..2]}
OS = (Processes:PROCESS || Processes::console:
  -> BSEMA)>>(user).
```

Dining Savages

The dining savages: A tribe of savages eats communal dinners from a large pot capable of holding M servings of stewed missionaries. When a savage wants to eat, he helps himself from the pot unless it is empty, in which case he waits until the cook refills the pot. If the pot is empty, the cook refills the pot with M servings. The behavior of the savages and the cook is described by

```
SAVAGE = (get_serving->SAVAGE).
COOK = (fill_pot->COOK).
```

Model the behaviour of the pot and of the system as FSP processes.

```
const M = 5
SAVAGE = (getserving -> SAVAGE).
COOK = (fillpot -> COOK).
POT = SERVINGS[0],
SERVINGS[i:10..M] = (when (i==0) fillpot ->
  SERVINGS[M] | when (i>0) getserving ->
  SERVINGS[i-1]).
|| SAVAGES = (SAVAGE || COOK || POT).
```

Simplified Multidimensional Semaphores

The extended primitives edown and eup are atomic (indivisible) and each operates on a set of semaphore variables which must be initiated with non-negative integer value. edown($S1, \dots, Sn$): if for all i , $1 \leq i \leq n$, $S_i > 0$ then for all i , $1 \leq i \leq n$, $S_i := S_i - 1$ else block execution of calling processes eup($S1, \dots, Sn$): if processes blocked on $(S1, \dots, Sn)$ then awaken one of them else for all i , $1 \leq i \leq n$, $S_i := S_i + 1$

```
SEM(N=INITIAL_VALUE = SEMA[N],
SEMA[v:Int] = (when (v>=Max) up -> SEMA[v+1] |
  when (v>0) down -> SEMA[v-1]).
SEMS1S2(INITIAL1=3, INITIAL2=3) = (S1:SEM(3) || S2:
  | S3:(SEM(3))\{S1.S2.up/S1.up, S1.S2.up/S2.up,
  | S1.S2.down/S1.down, S1.S2.down/S2.down, S1.down).
```

Two Warring Neighbours

Model this algorithm for two neighbours $n1$ and $n2$. Specified the required safety properties for the field and check that it does indeed ensure mutually exclusive access. Specify the required progress properties for the neighbours such that they both get to pick berries given a fair scheduling strategy.

```
const False = 0
const True = 1
range Bool = False..True
set BoolActions = {setTrue, setFalse, [False], [True]}
BOOLVAR = VAL[False],
VAL[v:Bool] = (setTrue -> VAL[True]
  | setFalse -> VAL[False]
  | [v] -> VAL[v]
  ).
||FLAGS = (flag1:BOOLVAR || flag2:BOOLVAR).
NEIGHBOUR1 = (flag1.setTrue -> TEST),
TEST = (flag2[Bool] -> NEIGHBOUR1)
  | if(b) then
    (flag1.setFalse -> NEIGHBOUR1)
  else
    (enter -> exit -> flag1.
      | setFalse -> NEIGHBOUR1
      | BoolActions).
NEIGHBOUR2 = (flag2.setTrue -> TEST),
TEST = (flag1[Bool] -> NEIGHBOUR2)
  | if(b) then
    (flag2.setFalse -> NEIGHBOUR2)
else
  (enter -> exit -> flag2.setFalse -> NEIGHBOUR2)
    | (flag1,flag2).BoolActions).
PROPERTY SAFETY = (n1.enter -> n1.exit -> SAFETY |
  n2.enter -> n2.exit -> SAFETY).
||FIELD = (n1:NEIGHBOUR1 || n2:NEIGHBOUR2 || (n1,
  n2):FLAGS || SAFETY).
PROGRESS ENTER1 = (n1.enter)
PROGRESS ENTER2 = (n2.enter)
||GREEDY = FIELD<<((n1,n2).{flag1,flag2}.setTrue).
```

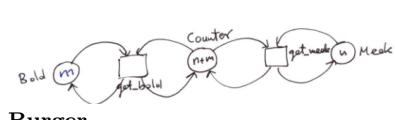
(b)[10]

A3Q2 - Gas Question

```
const N = 3 //number of customers
const M = 2 //number of pumps
range C = 1..N
range P = 1..M
range A = 1..2 //Amount of money or Gas
CUSTOMER = (prepay[A];A->gas[x;A]->CASHIER).
CASHIER = (customer[C];C->pump[X;A]->start[P][c];
  | x->CASHIER).
PUMP = (start[c;C|x;A]->gas[c;x]->DELIVER).
||STATION = (CASHIER || pump[1..M]:PUMP || DELIVER
  | |pump[1..M].start/start[i],
  pump[1..M].gas/gas[i]).
||GASSTATION = (customer[1..N]:CUSTOMER || STATION).
```

A3Q3 - Cheese Question

```
set Bold = {bold[1..2]}
set Meek = {meek[1..2]}
set Customers = {Bold,Meek}
CUSTOMER = (getcheese->CUSTOMER).
COUNTER = (getcheese->COUNTER).
||CHEESE_COUNTER = (Customers:CUSTOMER
  | |Customers::COUNTER).
```



Burger

A cook puts burgers in a pot. A client checks if there is at least one burger in the pot, and if so, the client must take one. Trace to error: fill[2], c2.check, fill[1], c1.check, c2.get, c1.get. Part b change pot to be:

```
POT = POT[0]
POT[p: Burgers] = (when (p>0) check -> get -> POT[p-1] | fill[n: Burgers] -> POT[n]).
```

CTL and LTL Examples

If the process is enabled infinitely often, then it runs infinitely often.

G F enabled \Rightarrow **AG**(**F** running)

AG(**A** enabled) \Rightarrow **AG**(**AF** running)

A passenger entering the elevator on 5th floor and pushing 2nd-floor button will never reach 6th floor, unless 6th-floor button is already lit or somebody will push it, no matter if she/he entered an upwards or upward travelling elevator.

AG(**floor = 5** \wedge **ButtonPressed2** \Rightarrow

A[\neg **floor = 6** \wedge **U****ButtonPressed6**])

Dining Philosophers with 'atomic' act of picking up both forks

```
FORK = (reserve_right -> take_right -> put_right
  | | reserve_left -> take_left -> put_left -> FORK).
PHIL = (think -> reserve_forks -> USE_FORKS).
USE_FORKS = (take_right -> take_left -> eat ->
  | | PUT_FORKS
  | | take_left -> take_right -> eat -> PUT_FORKS),
  | | PUT_FORKS = (put_left -> put_right -> PHIL).
  | | DINERS(N=5) = (forall[i:1..N] (phil[i]:PHIL ||
    | | (phil[i].right,phil[i+1..N].left)::FORK)
    | | reserve_forks/right.reserve_right,
    | | reserve_forks/left.reserve_left,
    | | reserve_forks_1/right.reserve_right_1,
    | | reserve_forks_1/left.reserve_left_1,
    | | reserve_forks_2/right.reserve_right_2,
    | | reserve_forks_2/left.reserve_left_2,
    | | reserve_forks_3/right.reserve_right_3,
    | | reserve_forks_3/left.reserve_left_3,
    | | reserve_forks_4/right.reserve_right_4,
    | | reserve_forks_4/left.reserve_left_4,
    | | reserve_forks_5/right.reserve_right_5,
    | | reserve_forks_5/left.reserve_left_5).
```